

Cell-Free MIMO-Assisted ISAC: Joint AP Switching and Power Allocation

Bin Yan¹, Zheng Wang¹, Amin Sakzad², Yongming Huang¹, and Michail Matthaiou³

¹Southeast University, Nanjing, China

²Monash University, Melbourne, Australia

³Queen's University, Belfast, U.K.

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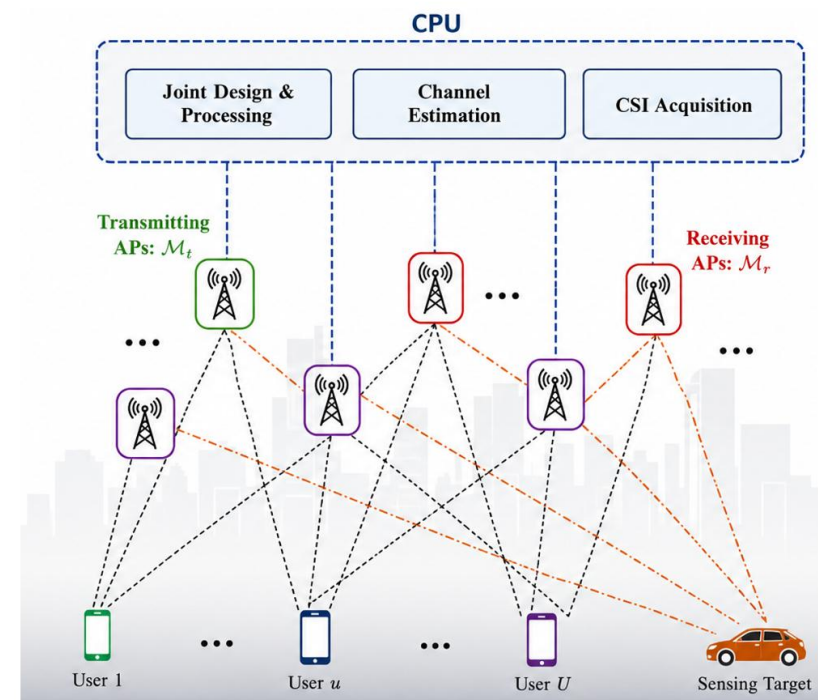
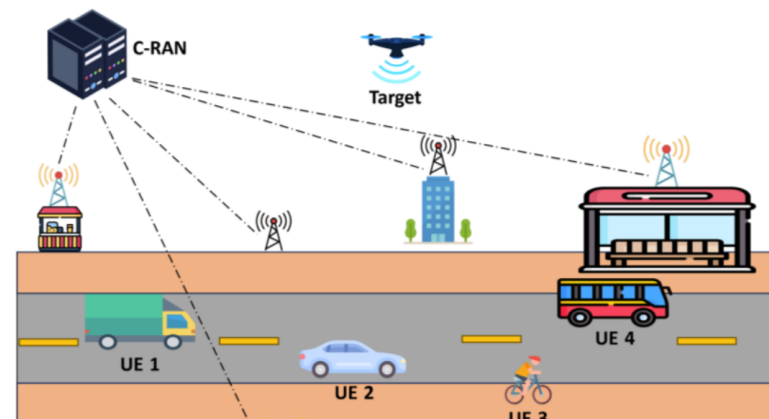
Limitations of centralized mMIMO-ISAC

With the evolution toward **B5G and 6G** wireless communication systems:

- Co-located antennas may cause uneven coverage.
- Inter-cell interference degrades both communication and sensing.

Challenges towards MIMO evolution

- **Distributed APs provide better spatial diversity.**
- **AP switching enables more flexible interference management.**



Dynamic AP mode switching

Communication AP (C-AP)

- Serve downlink users.
- Use partial zero-forcing precoding.
- Strong users: FZF precoding.
- Weak users: MRT precoding.

$$\mathbf{x}_m^c = \sum_{k \in \mathcal{S}_m} \sqrt{\rho_d \eta_{mk}^c} \mathbf{t}_{mk}^F x_k^c + \sum_{k \in \mathcal{W}_m} \sqrt{\rho_d \eta_{mk}^c} \mathbf{t}_{mk}^M x_k^c$$

Sensing AP (S-AP)

- Transmit probing signals.
- Illuminate multiple sensing zones.
- Use steering-vector-based beams.

$$\mathbf{x}_m^s = \sum_{l \in \mathcal{L}} \sqrt{\rho_d \eta_{ml}^s} \mathbf{a}_N(\theta_{ml}) x_{ml}^s$$

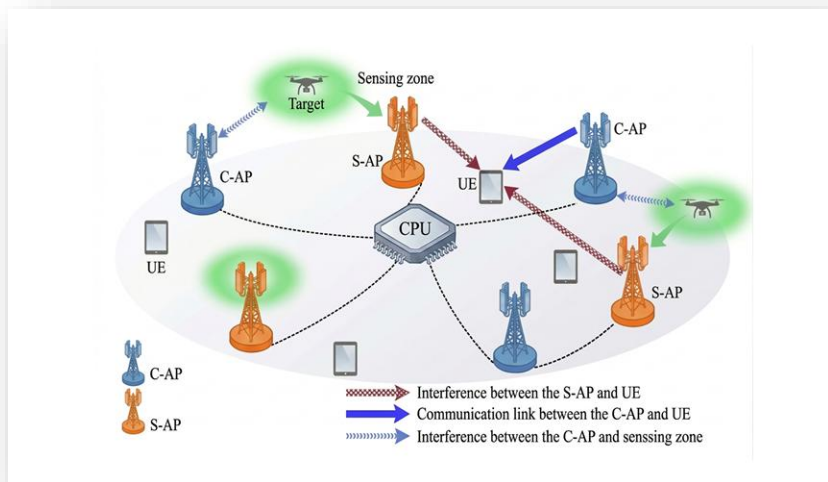


Fig. 1. Considered CF-mMIMO-assisted ISAC system.

Overall transmitted signal: $\mathbf{x}_m = a_m \mathbf{x}_m^c + (1 - a_m) \mathbf{x}_m^s$

Dynamic AP switching separates communication and sensing functions, reducing mutual interference and improving resource flexibility.



Communication: spectral efficiency (SE)

Use-and then-forget principle:

$$\text{SINR}_k(\Theta^c, \Theta^s) = \frac{\rho_d \left(\sum_{m \in \mathcal{M}} \sqrt{\eta_{mk}^c} \gamma_{mk} \varrho_{mk} \right)^2}{1 + \rho_d N \sum_{m \in \mathcal{M}} \sum_{l \in \mathcal{L}} \eta_{ml}^s \beta_{mk} + \rho_d \sum_{m \in \mathcal{M}} \sum_{k' \in \mathcal{K}} (\eta_{mk'}^c \gamma_{mk'} \varpi_{mk})}$$

Shannon's theorem:

$$\text{SE}_k(\Theta^c, \Theta^s) = \left(1 - \frac{\tau_u}{\tau} \right) \log_2 (1 + \text{SINR}_k(\Theta^c, \Theta^s))$$

- Dependent variable: C-AP and S-AP power allocation coefficient
- Other users' data + sensing signals act as effective noise.

Sensing: mainlobe-to-average-sidelobe ratio(MASR)

Minimize the sensing beampattern gain:

$$\text{MASR}_l \triangleq \frac{P_{\text{Sen,DS}}^{\text{ave}}(\theta_{t,ml})}{P_{\text{Com}}^{\text{ave}}(\theta_{t,m}) + P_{\text{SenDST}}^{\text{ave}}(\theta_{t,ml})}$$

$$\text{MASR}_l(\Theta^c, \Theta^s) = \frac{\sum_{m \in \mathcal{M}} N^2 \eta_{ml}^s}{\sum_{m \in \mathcal{M}} \sum_{k \in \mathcal{K}} \eta_{mk}^c \gamma_{mk} \nu_{mk} + \sum_{m \in \mathcal{M}} \sum_{l' \in \mathcal{L} \setminus l} \eta_{ml'}^s |\mathbf{a}_N^\dagger(\theta_{ml}) \mathbf{a}_N(\theta_{ml'})|^2}$$

- Average sensing power pattern distortion as well as communication distortion
- Users' data + other sensing zones sensing signals act as effective noise.



Problem Formulation

$$\mathcal{P}_1 : \max_{\mathbf{a}, \Theta^c, \Theta^s} \min_{k \in \mathcal{K}} \text{SE}_k(\Theta^c, \Theta^s)$$

$$\text{s.t. } \text{MASR}_l(\Theta^c, \Theta^s) \geq \kappa, \forall l \in \mathcal{L},$$

$$\sum_{k \in \mathcal{K}} \eta_{mk}^c \gamma_{mk} \nu_{mk} \leq a_m, \forall m \in \mathcal{M},$$

$$\sum_{l \in \mathcal{L}} \eta_{ml}^s \leq \frac{(1 - a_m)}{N}, \forall m \in \mathcal{M},$$

$$a_m \in \{0, 1\}, \forall m \in \mathcal{M}$$

Power
constraints

Description

Objective: Uniform QoS

s.t.: Achieve the desired MASR level

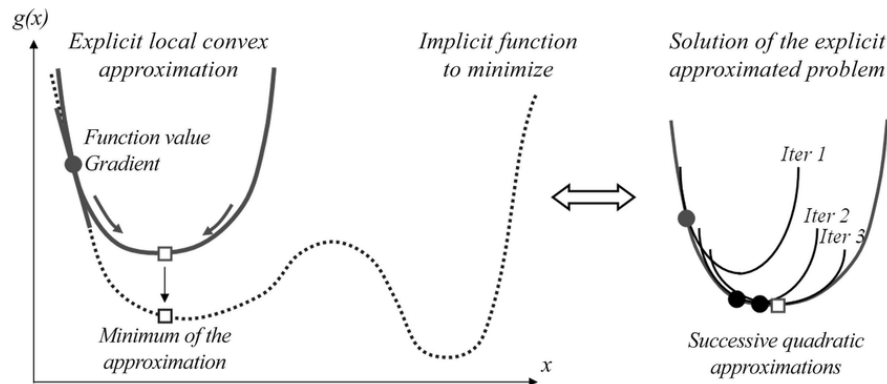
**Mixed integer
Non-convex
Optimization
Problem !**



Challenge

- **Variable properties:** Mixed integer problem, there are both integer variables and continuous variables.
- **Variable coupling:** There is a coupling property between integer variables and discrete variables.
- **Concavity:** Objective function and constrained height nonconvex.

Traditional solutions

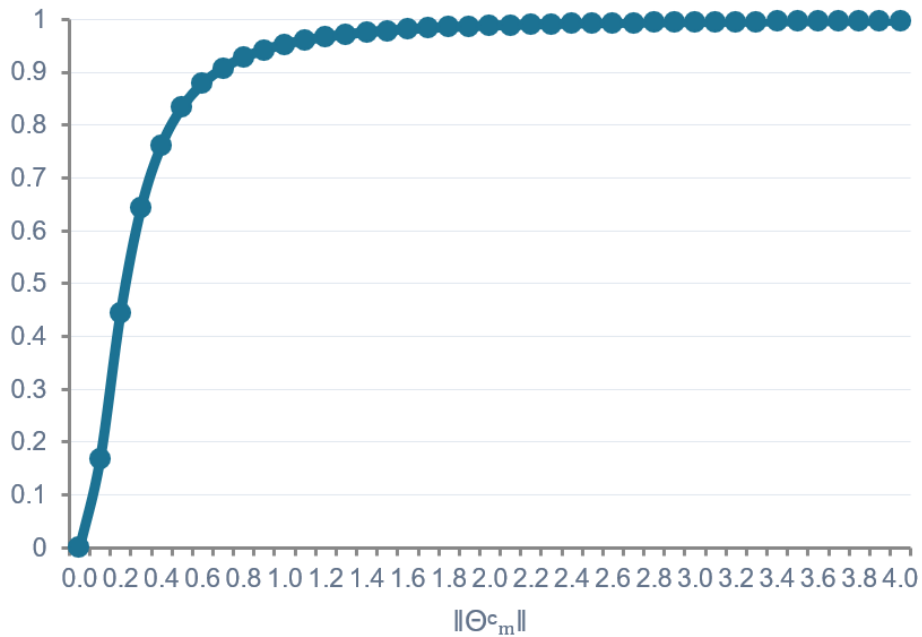


- Variable relaxation: $\{0,1\} \rightarrow [0,1]$
- Successive convex approximation (SCA) for Nonconvex Optimization

Unaffordable computational complexity!



KEY: use the coupling between discrete variables and continuous variables



P1 → P2: binary a_m removed; constraint becomes $N \sum_l \eta_{ml}^s \leq 1 - \sigma(\Theta_m^c)$

$\|\Theta_m^c\| = 0$, AP operates in sensing mode ($a_m = 0$)

$\|\Theta_m^c\| > 0 \iff a_m = 1$,
forming a step-function mapping (non-smooth).



$$\sigma(\Theta_m^c) = \frac{\|\Theta_m^c\|^2}{\|\Theta_m^c\|^2 + \delta}, \quad \Theta_m^c \in \mathbb{R}_+^{1 \times K}$$

Approximate characterization of discrete variables by continuous variables



Original problem

$$\begin{aligned}
 \mathcal{P}_1 : \quad & \max_{\mathbf{a}, \Theta^c, \Theta^s} \min_{k \in \mathcal{K}} \text{SE}_k(\Theta^c, \Theta^s) \\
 \text{s.t.} \quad & \text{MASR}_l(\Theta^c, \Theta^s) \geq \kappa, \forall l \in \mathcal{L}, \\
 & \sum_{k \in \mathcal{K}} \eta_{mk}^c \gamma_{mk} \nu_{mk} \leq a_m, \forall m \in \mathcal{M}, \\
 & \sum_{l \in \mathcal{L}} \eta_{ml}^s \leq \frac{(1 - a_m)}{N}, \forall m \in \mathcal{M}, \\
 & a_m \in \{0, 1\}, \forall m \in \mathcal{M},
 \end{aligned}$$

Problems after smooth representation

$$\begin{aligned}
 \mathcal{P}_2 : \quad & \max_{\Theta} f(\Theta) \triangleq \min_{k \in \mathcal{K}} \text{SINR}_k(\Theta) \\
 \text{s.t.} \quad & \text{MASR}_l(\Theta) \geq \kappa, \forall l \in \mathcal{L}, \\
 & \sum_{k \in \mathcal{K}} \eta_{mk}^c \gamma_{mk} \nu_{mk} \leq 1, \forall m \in \mathcal{M}, \\
 & N \sum_{l \in \mathcal{L}} \eta_{ml}^s \leq 1 - \frac{\|\Theta_m^c\|^2}{\|\Theta_m^c\|^2 + \delta}, \forall m \in \mathcal{M}.
 \end{aligned}$$

- Mixed integer and continuous
- Non-convex problem



- **Only continuous !**
- Non-convex problem
- Non-smooth objective function



Smoothing of the objective function

$$f(\Theta) = \min_{k \in \mathcal{K}} \text{SINR}_k(\Theta) \approx -f_\chi(\Theta)$$

$$\triangleq -\frac{1}{\chi} \log \left(\frac{1}{K} \sum_{k \in \mathcal{K}} \exp(-\chi \text{SINR}_k(\Theta)) \right),$$

$\chi > 0$ is the smoothness parameter.

$$f(\Theta) + \frac{\ln K}{\chi} \geq -f_\chi(\Theta) \geq f(\Theta).$$

- ***The objective function changes from non-smooth to smooth:*** making the gradient algorithm applicable
- ***Select appropriate smoothness parameter:*** prevent numerical spillover while ensuring high approximation



Take penalties to deal with constraints

$$Q_1(\Theta) \triangleq \sum_{l \in \mathcal{L}} [\max(0, \kappa - \text{MASR}_l(\Theta))]^2,$$

$$Q_2(\Theta) \triangleq \sum_{m \in \mathcal{M}} \left[\max \left(0, N \sum_{l \in \mathcal{L}} \eta_{ml}^s + \frac{\|\Theta_m^c\|^2}{\|\Theta_m^c\|^2 + \delta} - 1 \right) \right]^2.$$

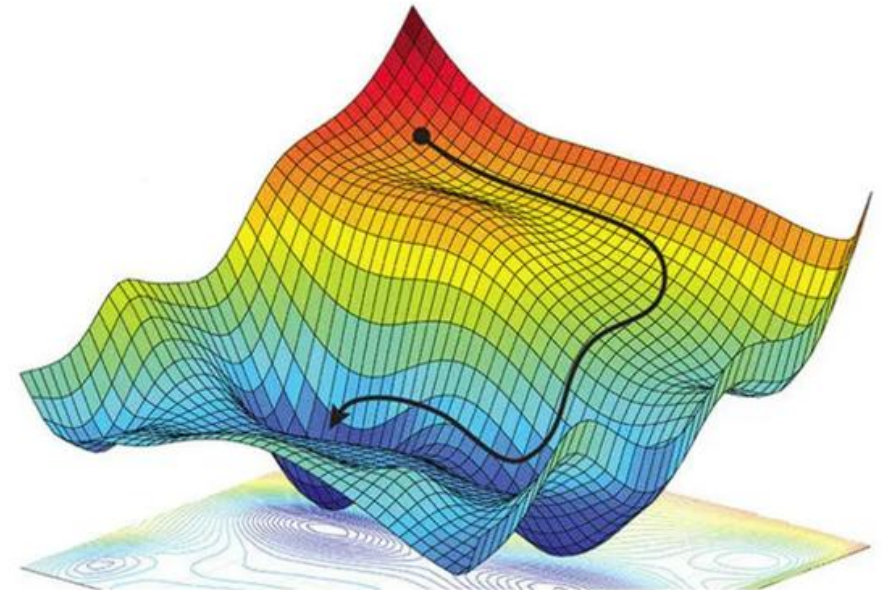
Final objective function

$$H_{\chi, \lambda}(\Theta) \triangleq f_{\chi}(\Theta) + \sum_{i=1}^2 \lambda_i \mu_i Q_i(\Theta).$$

Non-convex smooth + convex non-smooth

$$\mathcal{P}_3 : \min_{\Theta} H_{\chi, \lambda}(\Theta) + I(\Theta^c).$$

The proximal gradient method is suitable!





Core renewal formula of near end gradient method

$$\Theta^{(t)} = \text{prox}_{\alpha^{(t)}, I} \left(\mathbf{Z}^{(t)} - \alpha^{(t)} \nabla H_{\chi, \lambda}(\mathbf{Z}^{(t)}) \right),$$

Smooth term: standard gradient descent



$$\text{prox}_{\mathcal{C}}(\mathbf{X}) = \arg \min_{\Theta \in \mathcal{C}} \|\Theta - \mathbf{X}\|^2,$$

Non-smooth term: using convexity to simplify to nearest distance optimization problem



$$\text{prox}_{\mathcal{C}}(\mathbf{X}) = \text{prox}_{\mathcal{C}}(\tilde{\mathbf{X}}) = \arg \min_{\Theta^c \in \mathcal{C}} \|\Theta^c - \tilde{\mathbf{X}}\|^2$$

Projection further simplified: only related to communication AP power allocation coefficient



Lemma 1. For given $\tilde{\mathbf{X}}$, the projection $\text{prox}_c(\tilde{\mathbf{X}})$ for the communication PAC is given by the following analytical solution

$$\eta_{mk}^{c,*} = \max\left(0, \tilde{x}_{mk} - \frac{\xi_m}{2} \gamma_{mk} \nu_{mk}\right). \quad (24)$$

Here, \tilde{x}_{mk} is the (m, k) -th entry of $\tilde{\mathbf{X}}$ and ξ_m is the Lagrange multiplier determined according to the following condition

$$\xi_m = \begin{cases} 0, & \text{if } \sum_{k \in \mathcal{K}} \max(0, \tilde{x}_{mk}) \gamma_{mk} \nu_{mk} \leq 1, \\ \text{the root of (29),} & \text{otherwise.} \end{cases} \quad (25)$$

$$\sum_{k \in \mathcal{K}} \max\left(0, \tilde{x}_{mk} - \frac{\xi_m}{2} \gamma_{mk} \nu_{mk}\right) \gamma_{mk} \nu_{mk} = 1, \quad (29)$$

which is continuous and strictly decreasing in ξ_m . This solution essentially corresponds to a soft-thresholding operation, where the value of ξ_m can be efficiently obtained using bisection search or fixed-point iteration.

Algorithm 1: The SC-JAPSPA algorithm for \mathcal{P}_3

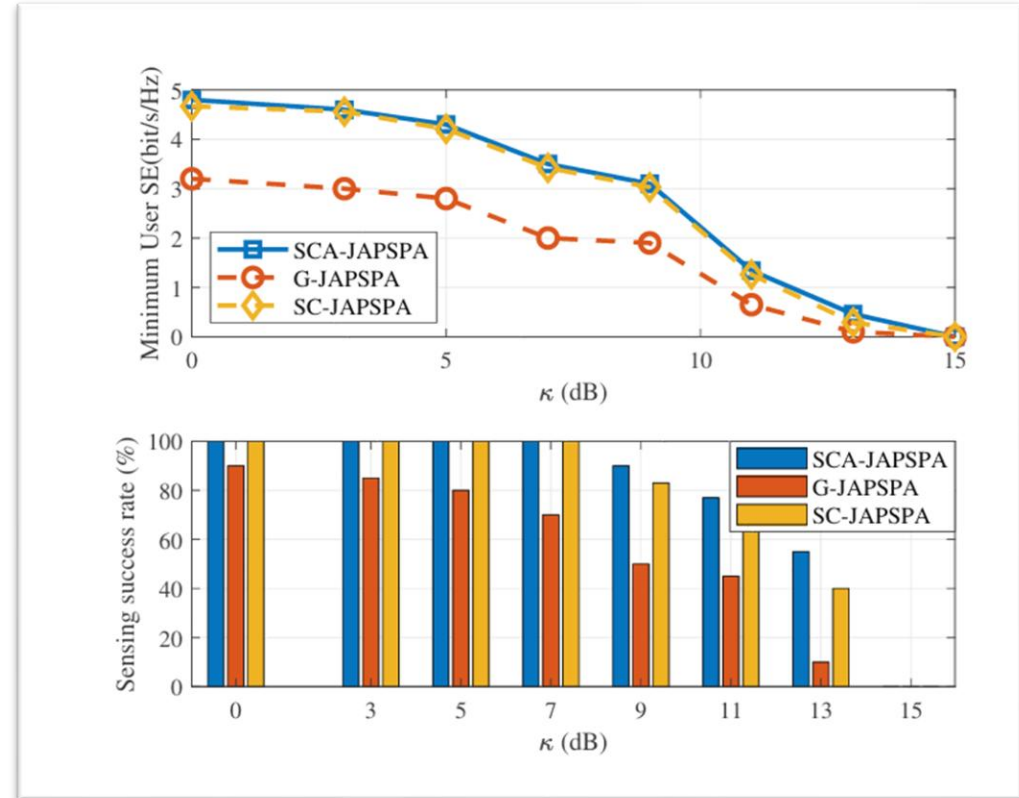
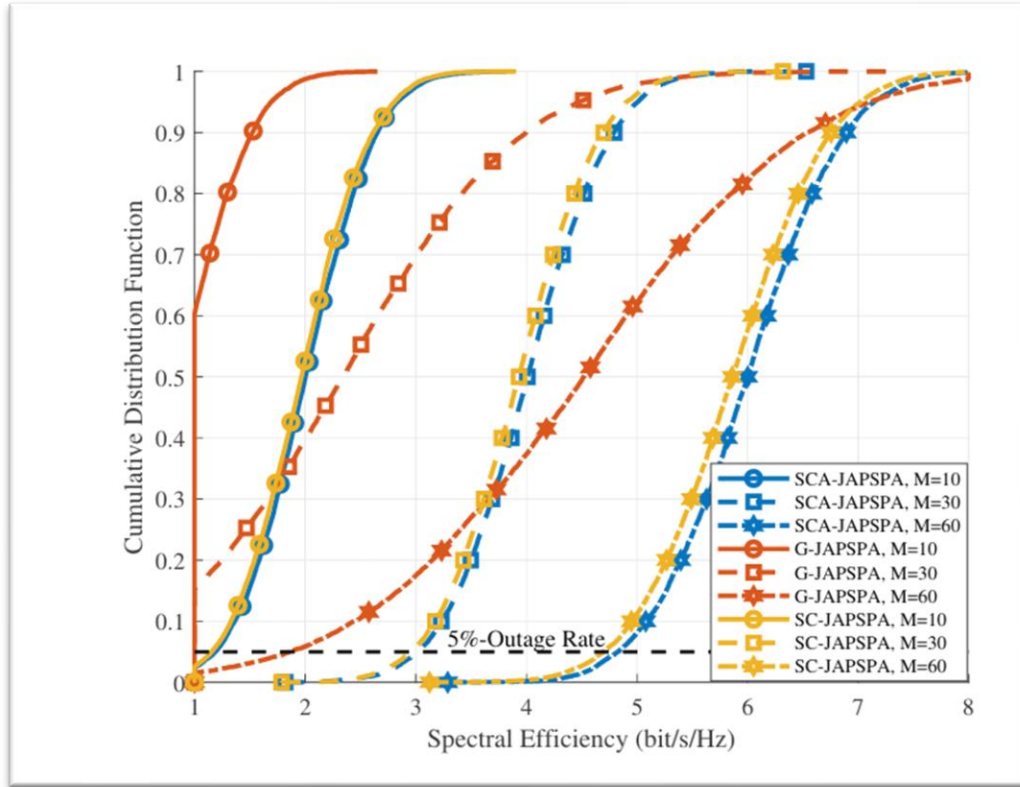
Input : $\mathbf{Z}^{(1)} = \Theta^{(0)}, \mu_1 = 10^3, \mu_2 = 10, \beta = 2, \omega = 0.5, \lambda = 1, t = 1, \varepsilon = 10^{-3}, \alpha^{(t)} = 10^{-3}$

```

1 repeat // Penalty loop
2   repeat // APG-AM loop
3     update  $\Theta^{(t)}$  via (21) and  $\mathbf{v}^{(t)}$  via (30)
4     update  $\mathbf{Z}^{(t+1)}$  and  $\beta$  via (31)
5     if  $|H_{\chi, \lambda}(\Theta^{(t)}) - H_{\chi, \lambda}(\Theta^{(t-1)})| > \varepsilon$  then
6       |  $t = t + 1$ 
7     end
8   until  $|H_{\chi, \lambda}(\Theta^{(t)}) - H_{\chi, \lambda}(\Theta^{(t-1)})| \leq \varepsilon$ ;
9   increase the penalty coefficients  $\lambda_i = 10\lambda_i, i = 1, 2$ 
10 until  $|Q_1(\Theta^{(t)}) - Q_1(\Theta^{(t-1)})| \leq \varepsilon$  as well as
     $|Q_2(\Theta^{(t)}) - Q_2(\Theta^{(t-1)})| \leq \varepsilon$ ;
Output: Stationary power allocation coefficients:  $\Theta^*$ 

```

- Introducing auxiliary variables for *momentum acceleration*
- *Smooth Lipschitz*: monotonically converges to the stationary point



- SC-JAPSPA provides near-SCA communication performance with better reliability than G-JAPSPA.
- SC-JAPSPA achieves a robust tradeoff between minimum user SE and sensing success rate.



TABLE I
COMPARISON BETWEEN THE EXECUTION TIME (IN SECONDS)

Algorithm	Number of APs (M)				Number of Users (K)				Number of Sensing Zones (L)			
	20	30	40	60	4	8	12	20	2	4	8	12
SCA-JAPSPA [1]	173.61	269.93	375.27	424.84	152.64	173.61	213.43	284.31	143.59	173.61	202.86	243.03
G-JAPSPA [1]	25.88	31.15	35.21	58.23	17.95	25.88	33.43	45.34	15.28	25.88	31.07	37.29
SC-JAPSPA (this work)	8.57	14.68	19.34	25.93	4.13	8.57	13.85	17.34	3.02	8.57	11.39	14.51

$$\text{SC-JAPSPA: } \mathcal{O}(M \max(K, L)^2)$$

\ll

$$\text{SCA-JAPSPA: } \mathcal{O}(M^{3.5} \max(K, L)^{3.5})$$

➤ SC-JAPSPA achieves near-benchmark performance with much lower runtime and complexity.

Thank You for Your Attention

Bin Yan¹, Zheng Wang¹, Amin Sakzad², Yongming Huang¹, and Michail Matthaiou³

¹Southeast University, Nanjing, China

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